

# PHYSICS 2DL – SPRING 2010

## MODERN PHYSICS LABORATORY

Monday May 3, 2010

Course Week 6

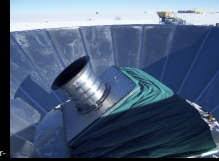
Lab Week

Prof. Brian Keating





# Galileo between Science, Science Studies and Science Fiction



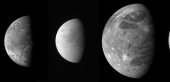
In his recent book, *Galileo's Dream*, Kim Stanley Robinson creates a portrait of Galileo's life in which he combines historic research with science fiction tropes to show the impact and challenges of paradigm shifts and their very human origins. One of the sources for this work is the research of Mario Biagioli, who will discuss the importance of Robinson's approach to historians of science and interrelationships between science studies and science fiction. Additionally, UCSD Professor of Physics Brian Keating will describe his observations of the early universe made with a version of Galileo's refractor telescope, which is sensitive to radio-waves, instead of visible light. This telescope located in Antarctica, has made ultra-sensitive images of the afterglow of the Big Bang. He will show images of the early universe as well as data from observations of Jupiter made with a new UCSD telescope, and will discuss techniques to peer deeper into the universe, standing on Galileo's shoulders. All will be framed by films of high resolution images produced by Sheldon Brown of the four Jovian moons discovered by Galileo some 400 years ago. This event is organized by Don Wayne, Provost of Revelle College.

**MARIO BIAGIOLI, SHELDON BROWN, ... BRIAN KEATING, ... KIM STANLEY ROBINSON**

**Mario Biagioli** is Professor of the History of Science at Harvard University. After studying computer science at the University of Pisa (Italy) and receiving his MFA in photography from the Visual Studies Workshop/RIT (Rochester, NY), he was awarded a PhD in history of science from UC Berkeley in 1989. His work has focused mostly on the place of science and discovery in the baroque court, and the uses of instruments, imaging techniques, and the tactical uses of print, spectacle, and display in the making of knowledge (*Galileo Courter* (Chicago, 1993 – translated in German, Greek, Spanish, and Portuguese) and *Galileo's Instruments of Credit* (Chicago, 2006)). Along with a standing interest in the scientific revolution, he has also explored more modern topics, like Nazi science, science museums, as well as methodological debates concerning science studies and their relationship with the humanities. A Guggenheim Fellowship allowed him to develop an additional research focus on the history and philosophy of intellectual property and on the author function in science from 1600 to 'big science.' He is now working on "Claiming the New" – a book on intellectual property in science. He is also the editor of *The Science Studies Reader* (Routledge, 1998), and (with Jessica Riskin) of *Nature Engaged* (Palgrave/McMillan, in press).

**Sheldon Brown** is the Director of the Center for Research in Computing and the Arts (CRCA) at the University of California at San Diego (UCSD) where he is a Professor of Visual Arts. He is the Site Director of the UCSD branch of the NSF sponsored Center for Hybrid Multicore Productivity Research leading its focus on next generation digital media research. He founded the New Media Arts area for the California Institute of Telecommunications and Information Technologies (Calit2), and is currently the Calit2 Artist-in-Residence. His artwork examines the relationships between mediated and physical experiences, and explores the interconnections between media such as: computer gaming, virtual worlds, cinema, installation, public art, and sculpture. He has shown his work at such places as The Museum of Contemporary Art in Shanghai, The Exploratorium in San Francisco, Ars Electronica in Linz Austria, The Klippen in NYC, Zacheta Gallery in Warsaw, Centro Nacional in Mexico City, The National Academy of Science in Washington DC, and others. He has been commissioned for public artworks in Seattle, San Francisco, San Diego and Mexico City, and has received grants from AT&T, New Experiments in Art and Technology, the NEA, the NSF, the Rockefeller Foundation, IBM, Intel, Sun, Vicon and others.  
<http://sheldonbrown.com/>

UCSD graduate **Kim Stanley Robinson** is a well-known science fiction writer. Author of the Mars trilogy (*Red Mars*, *Green Mars*, *Blue Mars*), his novels and short stories have been translated into twenty-three languages, and have been given Hugo and Nebula awards, as well as awards in England, France, Spain, and Japan. In 1995 he went to Antarctica as part of the U.S. National Science Foundation's Antarctic Artists and Writers' Program, and in 2008 he joined the Sequoia Parks Foundation's Artists In the Back Country program. Last year *Time* magazine named him one of their "Heroes of the Environment." He serves on the advisory boards of the Clarion Writer's Workshop, the Planetary Society, the Mars Association, and UCSD's Sixth College. This September he will be the guest of honor at the World Science Fiction Convention, in Melbourne, Australia.



**Professor Brian Keating** (PhD, Brown University 2000) is an astrophysicist with UCSD's Department of Physics and the Center for Astrophysics and Space Sciences. He guides a research team of undergraduates, graduate students, and Post-docs to develop sensitive instrumentation to study the early universe in the radio-, microwave- and infrared-wavelength regions of the electromagnetic spectrum. He holds a U.S. Patent for a novel microwave polarization modulator. Keating completed postdoctoral research at Stanford University and was an NSF Postdoctoral Fellow at Caltech before coming to UCSD in 2004. In 2007 he received the Presidential Early Career Award for Scientists and Engineers at the White House from President George W. Bush for his work on a telescope he designed and fielded with his students and colleagues at the US Amundsen-Scott South Pole Research Station.

**Thursday, May 6, 2010**  
**4:30—6:00 p.m.**  
**Calit2, Atkinson Hall**

*Co-Sponsored by*  
*California Institute for Telecommunications and Information Technology (Calit2)*  
*Clarion Writers' Workshop*  
*Center for Research in Computing and the Arts (CRCA)*  
*The Council of Provosts*  
*Department of Literature*  
*Division of Arts and Humanities*  
*Division of Physical Sciences*  
*Revelle College*



In commemoration of the 400th year anniversary of Galileo's telescope, the Literature Department is pleased to present...

## MARIO BIAGIOLI

### ► *Inventing Invention: Galileo's Telescope Between Science and Craft*

**TUESDAY, May 4, 2010**

**6:00 p.m.**

**The Atkinson Pavilion at the  
Faculty Club  
UC San Diego**

***Followed by a reception***

***The lecture will be in  
English***

***Free and open to the public***

Galileo's name is routinely associated with the telescope, and vice versa. As obvious as this link may sound today, it is in fact the result of historical narratives - narratives initiated by Galileo himself. He did not invent the telescope but Galileo's telescope. His instrument, Galileo intimated, was different from all others because of the way it had been invented (through theory, not haphazard practice) and because of the unprecedented astronomical discoveries it made possible: the irregularities of the lunar surface, the satellites of Jupiter, and many more fixed stars. Galileo's claim to the inventorship of the telescope was therefore tied - necessarily so - to what he presented as the unique features of his instrument and the modalities of its invention. In the Binder Lecture, Professor Biagioli will argue that Galileo constructed his originality and that of his instruments through narratives that were themselves original, in a variety of ways.



# 2Day in 2DL

- Questions/Announcements
- Error Analysis: Review Ch 6 (rejecting data) Ch 7 weighted averages; NEW! Ch8 least squares fitting.
- HW due in lab this week
- Special Topic: Franck-Hertz: Using Data Acquisition to improve your life.

# New Today Ch 8

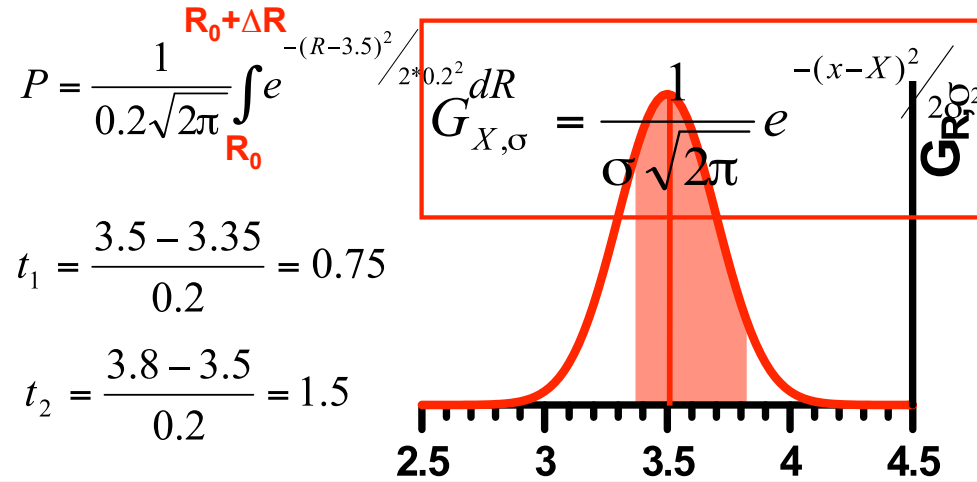
- Ch 6,7 Review
- Ch 8 = Least Squares fitting

## Final example

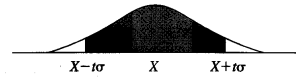
A student makes several measurements of a resistance  $R$  and determines  $\bar{R}=3.5\Omega$  and  $\sigma_R=0.2\Omega$ .

Write an expression for the probability of obtaining a measured value between  $R_0$  and  $R_0+\Delta R$ .

What is the probability of obtaining a measured value between  $3.35\Omega$  and  $3.8\Omega$ ?



**Table A.** The percentage probability,  
 $Prob(\text{within } t\sigma) = \int_{X-t\sigma}^{X+t\sigma} G_{X,\sigma}(x) dx,$   
 as a function of  $t$ .



**t=1.5**

Then divide by 2  
 and add to  
 previous  
 (t=0.75 sigma)  
 probability.

t	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.00	0.80	1.60	2.39	3.19	3.99	4.78	5.58	6.38	7.17
0.1	7.97	8.76	9.55	10.34	11.13	11.92	12.71	13.50	14.28	15.07
0.2	15.85	16.63	17.41	18.19	18.97	19.74	20.51	21.28	22.05	22.82
0.3	23.58	24.34	25.10	25.86	26.61	27.37	28.12	28.86	29.61	30.35
0.4	31.08	31.82	32.55	33.28	34.01	34.73	35.45	36.16	36.88	37.59
0.5	38.29	38.99	39.69	40.39	41.08	41.77	42.45	43.13	43.81	44.48
0.6	45.15	45.81	46.47	47.13	47.78	48.43	49.07	49.71	50.35	50.98
0.7	51.61	52.23	52.85	53.46	54.07	54.67	55.27	55.87	56.46	57.05
0.8	57.63	58.21	58.78	59.35	59.91	60.47	61.02	61.57	62.11	62.65
0.9	63.19	63.72	64.24	64.76	65.28	65.79	66.29	66.80	67.29	67.78
1.0	68.27	68.75	69.23	69.70	70.17	70.63	71.09	71.54	71.99	72.43
1.1	72.87	73.30	73.73	74.15	74.57	74.99	75.40	75.80	76.20	76.60
1.2	76.99	77.37	77.75	78.13	78.50	78.87	79.23	79.59	79.95	80.29
1.3	80.64	80.98	81.32	81.65	81.98	82.30	82.62	82.93	83.24	83.55
1.4	83.85	84.15	84.44	84.73	85.01	85.29	85.57	85.84	86.11	86.38
1.5	86.64	86.90	87.15	87.40	87.64	87.89	88.12	88.36	88.59	88.82
1.6	89.04	89.26	89.48	89.69	89.90	90.11	90.31	90.51	90.70	90.90
1.7	91.09	91.27	91.46	91.64	91.81	91.99	92.16	92.33	92.49	92.65
1.8	92.81	92.97	93.12	93.28	93.42	93.57	93.71	93.85	93.99	94.12
1.9	94.26	94.39	94.51	94.64	94.76	94.88	95.00	95.12	95.23	95.34
2.0	95.45	95.56	95.66	95.76	95.86	95.96	96.06	96.15	96.25	96.34
2.1	96.43	96.51	96.60	96.68	96.76	96.84	96.92	97.00	97.07	97.15
2.2	97.22	97.29	97.36	97.43	97.49	97.56	97.62	97.68	97.74	97.80
2.3	97.86	97.91	97.97	98.02	98.07	98.12	98.17	98.22	98.27	98.32
2.4	98.36	98.40	98.45	98.49	98.53	98.57	98.61	98.65	98.69	98.72
2.5	98.76	98.79	98.83	98.86	98.89	98.92	98.95	98.98	99.01	99.04
2.6	99.07	99.09	99.12	99.15	99.17	99.20	99.22	99.24	99.26	99.29

## Chapter 7 Averaging Data

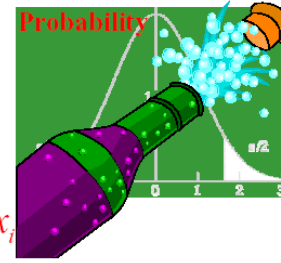
- Random Errors can be reduced by repeated measurements.
- The best estimate of the true value of a measured quantity is the average (mean).
- We can also estimate the RMS error from the set of measurements.
- We can then compute the error on the mean which decreases with the number of measurements.

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$\sigma_x^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

$$\sigma_{\bar{x}} = \frac{\sigma_x}{\sqrt{n}}$$

If  $\sigma_x$  is 1 mm, how many times must I measure to get a 0.2 mm error on the mean?

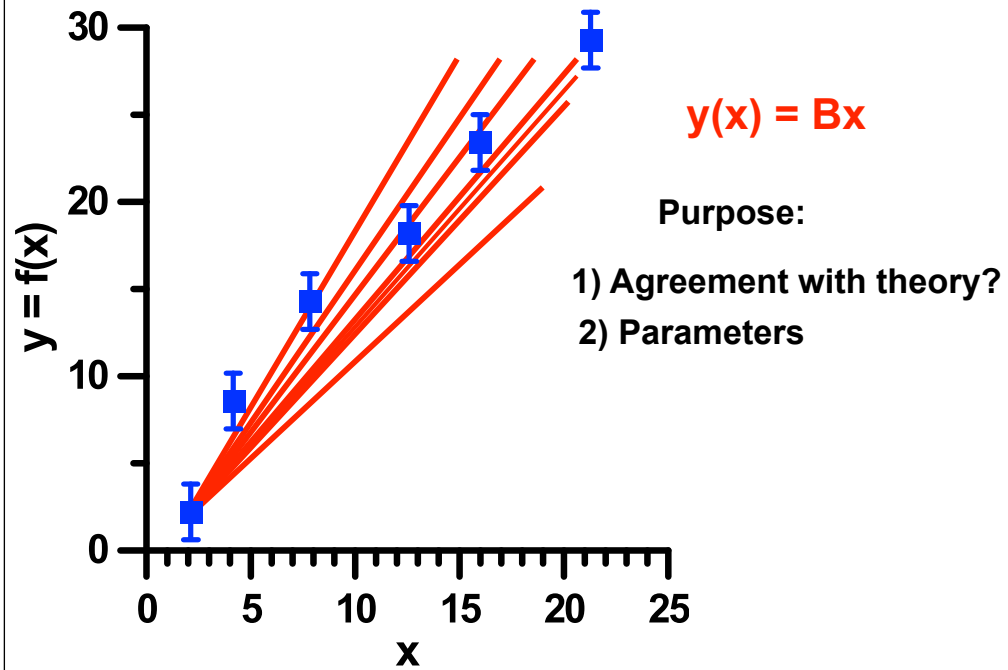




# New Today Ch 8

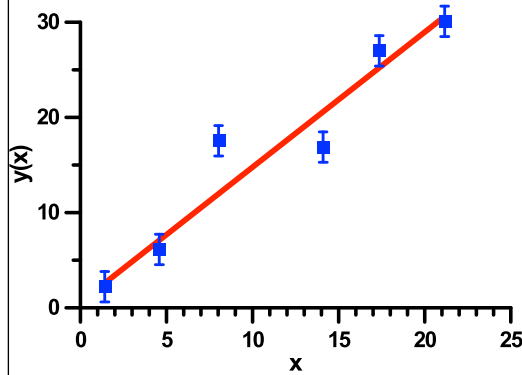
- Ch 6,7 Review
- Ch 8 = Least Squares fitting

# LEAST SQUARES FITTING (Ch.8)



Least Sq. Fits : Derived from:  $\chi^2$  TEST for FIT (Ch 12)

$$\chi^2 = \frac{\sum_{j=1}^N (y_j - f(x_j))^2}{\sigma_y^2} \cong \frac{N\sigma_y^2}{\sigma_y^2} = N$$



$$\tilde{\chi}^2 = \frac{\chi^2}{d} \cong 1$$

$d$  → # of degrees of freedom

# LEAST SQUARES FITTING

$$y=A+Bx+Cx^2+Dx^3+\dots+ Zx^N$$

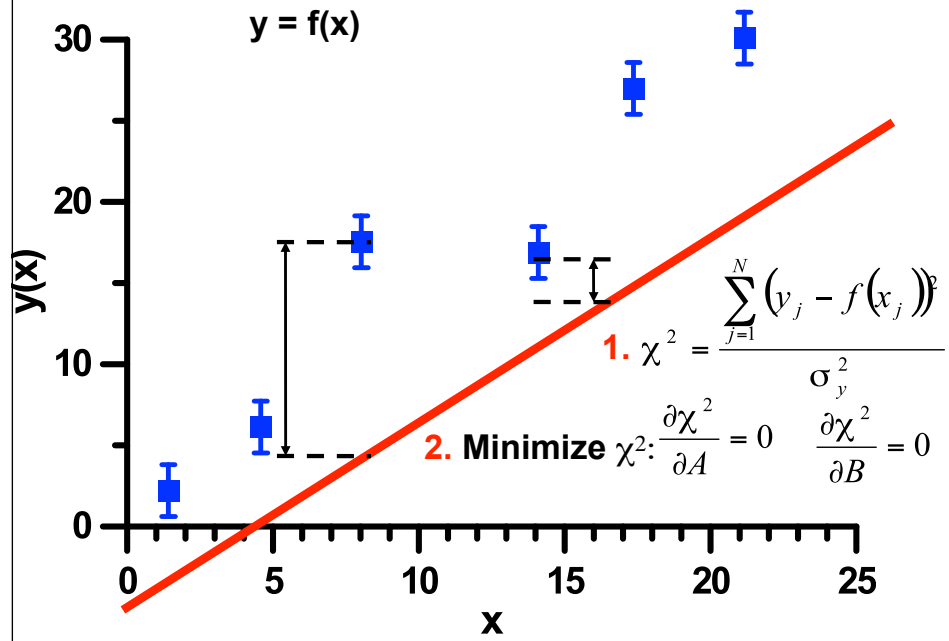
minimize  $\rightarrow \sum_{j=1}^N (y_j - f(x_j))^2$



$$\frac{\partial \sum_{j=1}^N (y_j - f(x_j))^2}{\partial A} = 0 \quad \frac{\partial \sum_{j=1}^N (y_j - f(x_j))^2}{\partial B} = 0 \quad \frac{\partial \sum_{j=1}^N (y_j - f(x_j))^2}{\partial C} = 0 \quad \dots$$

$\rightarrow$  **A,B,C...**

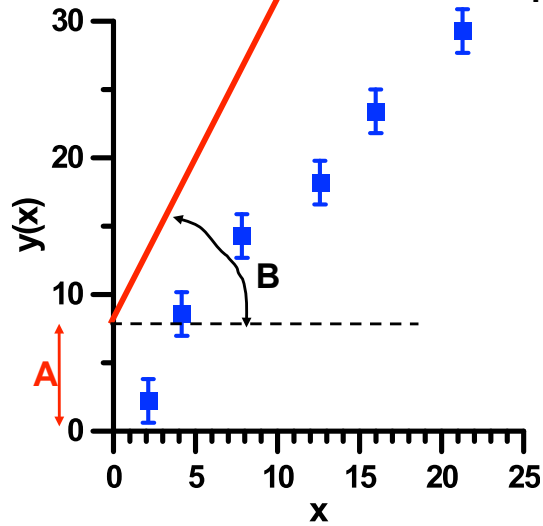
# LEAST SQUARES FITTING



# LINEAR FIT

$$y(x) = A + Bx :$$

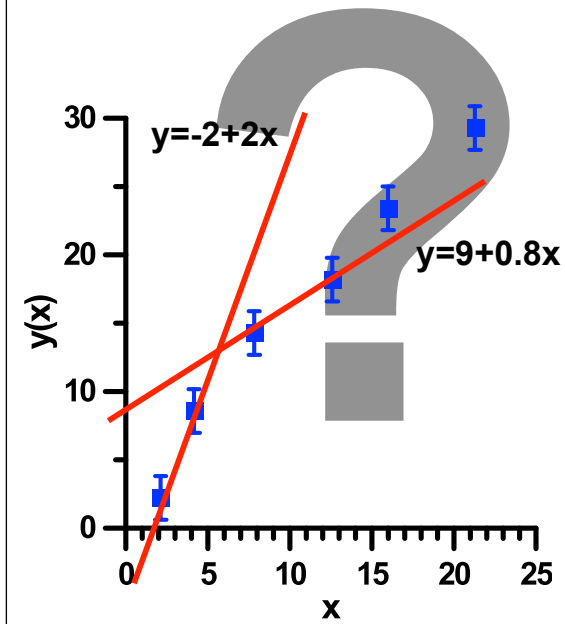
velocity at const acceleration  
Ohm's law  
many other...



x1	y1
x2	y2
x3	y3
x4	y4
x5	y5
x6	y6

# LINEAR FIT

$$y(x) = A + Bx$$

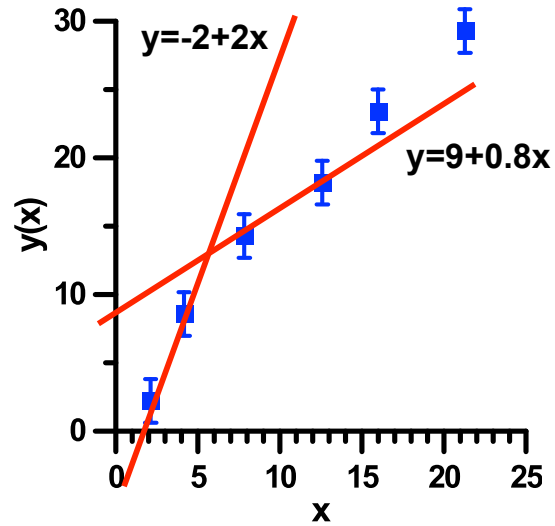


x1	y1
x2	y2
x3	y3
x4	y4
x5	y5
x6	y6

# LINEAR FIT

$$y(x) = A + Bx$$

x1	y1
x2	y2
x3	y3
x4	y4
x5	y5
x6	y6

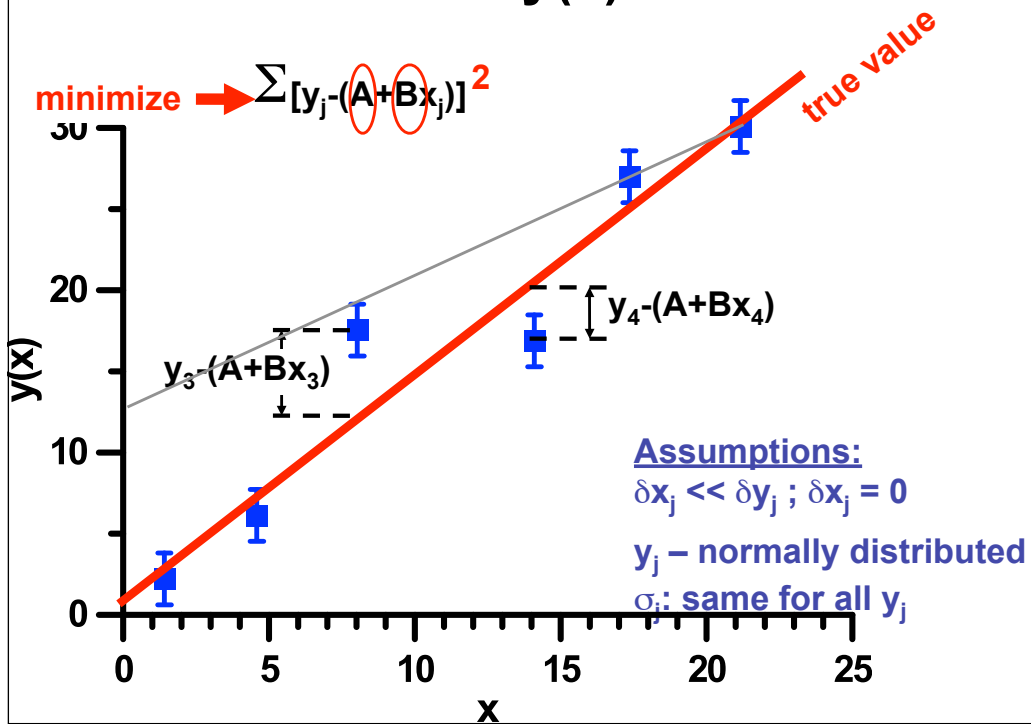


## Assumptions:

- 1)  $\delta x_j \ll \delta y_j$ ;  $\delta x_j = 0$
- 2)  $y_j$  – normally distributed
- 3)  $\sigma_j$ : same for all  $y_j$



# LINEAR FIT: $y(x) = A + Bx$

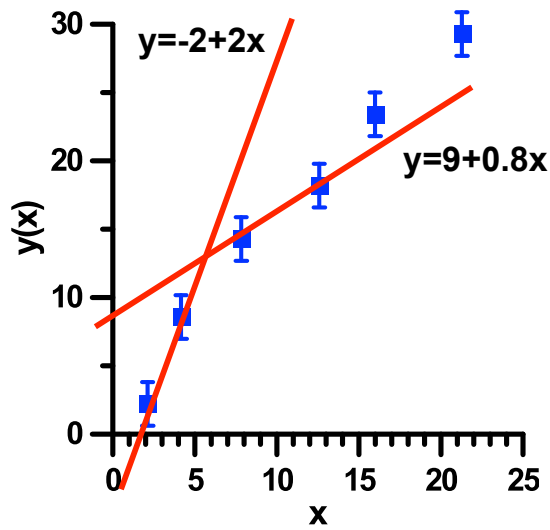


# LINEAR FIT

$$y(x) = A + Bx$$

true value  
of y

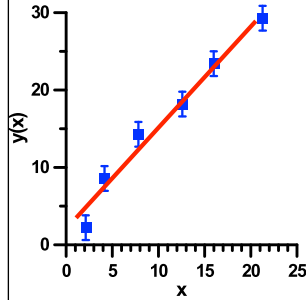
x1	y1
x2	y2
x3	y3
x4	y4
x5	y5
x6	y6



## Assumptions:

- 1)  $\delta x_j \ll \delta y_j ; \delta x_j = 0$
- 2)  $y_j$  - normally distributed
- 3)  $\sigma_j$ : same for all  $y_j$

# LINEAR FIT: $y(x) = A + Bx$



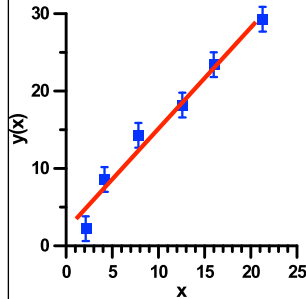
$$\begin{aligned} \text{Pr ob}(y_j) &\propto \frac{1}{\sigma_y} \exp\left[-\frac{(y_j - y_{true})^2}{2\sigma_y^2}\right] \\ &= \frac{1}{\sigma_y} \exp\left[-\frac{(y_j - A - Bx_j)^2}{2\sigma_y^2}\right] \end{aligned}$$

$$\text{Pr ob}(y_1, y_2, \dots, y_N) = \text{Pr ob}(y_1) \times \text{Pr ob}(y_2) \times \dots \times \text{Pr ob}(y_N)$$

$$\begin{aligned} &= \frac{1}{\sigma^N} \exp\left[\frac{-(y_1 - A - Bx_1)^2}{2\sigma_y^2} + \dots + \frac{-(y_N - A - Bx_N)^2}{2\sigma_y^2}\right] \\ &= \frac{1}{\sigma^N} \exp\left[\sum_{j=1}^N \frac{-(y_j - A - Bx_j)^2}{2\sigma_y^2}\right] \end{aligned}$$

$$\text{Best estimates of A\&B} \rightarrow \max \text{Prob}(y_1 \dots y_N) \rightarrow \min \sum [y_j - (A + Bx_j)]^2$$

# LINEAR FIT: $y(x) = A + Bx$



In Taylor p. 197

$$\frac{\partial \sum (y_j - A - Bx_j)^2}{\partial A} = 0$$

$$\frac{\partial \sum (y_j - A - Bx_j)^2}{\partial B} = 0$$



$$A = \frac{\sum x_j^2 \sum y_j - \sum x_j \sum x_j y_j}{N \sum x_j^2 - (\sum x_j)^2}$$

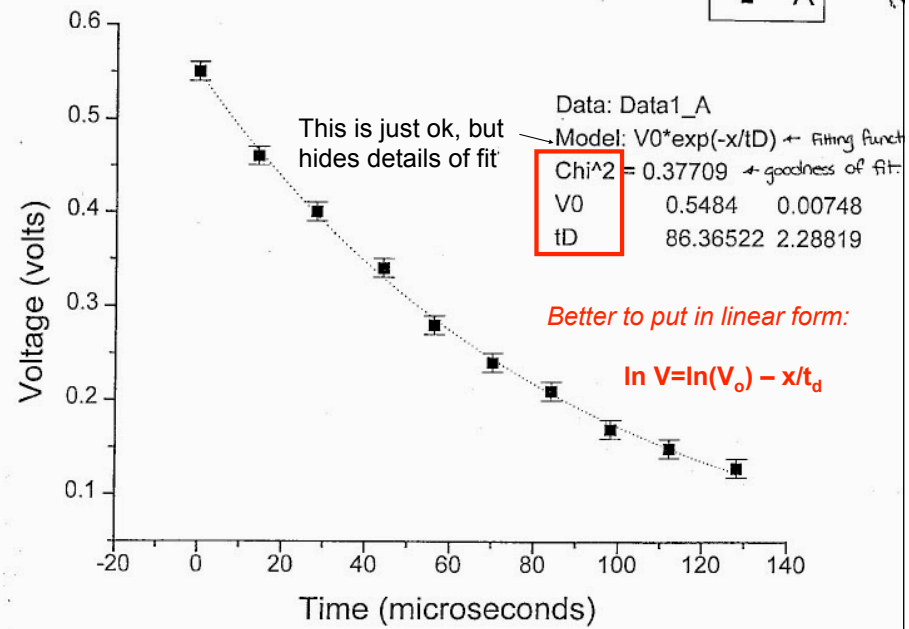
$$B = \frac{N \sum x_j y_j - \sum x_j \sum y_j}{N \sum x_j^2 - (\sum x_j)^2}$$

Best estimates of A&B  $\rightarrow$  max Prob( $y_1 \dots y_N$ )  $\rightarrow$  min  $\sum [y_j - (A + Bx_j)]^2$

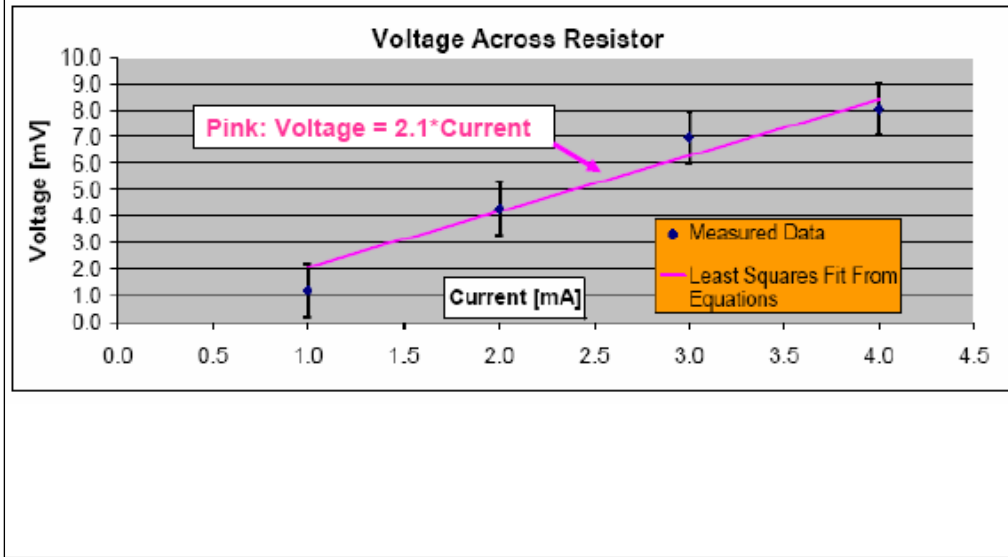
# LEAST SQUARES FITTING

Title : Voltage vs. Time

■ A



Here's our "final" example of the general technique when fitting for



## Fitting Voltage Data to $V=IR$

$$\frac{\partial \chi^2}{\partial R} = 0$$

*IMPLIES :*

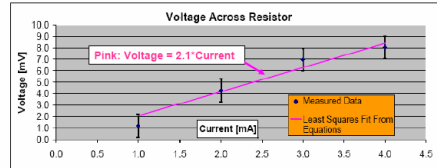
$N$  = number of data points. In this example,  $N=4$

$$R = \frac{\sum_i^N I_i V_i}{\sum_i^N I_i^2}$$

See Taylor

Problem 8.18

**Don't Use Linear fit with  $A=0$ !**



## What is the Error on the Best-Fit Parameter R?

Our general formula, which always applies, is:

$$\sigma_R = \sqrt{\left(\frac{\partial R}{\partial V_1}\right)^2 \sigma_{v_1}^2 + \left(\frac{\partial R}{\partial V_2}\right)^2 \sigma_{v_2}^2 + \dots + \left(\frac{\partial R}{\partial V_N}\right)^2 \sigma_{v_N}^2}$$

Since:  $\left(\frac{\partial R}{\partial V_1}\right)^2 = I_1^2, \left(\frac{\partial R}{\partial V_N}\right)^2 = I_N^2$

and:  $\sigma_{v_N} = 1mV$

Putting it all together:

$$so: \sigma_R = \frac{1mV \sqrt{\sum_i^N I_i^2}}{\sum_i^N I_i^2}$$

Check units are right, error has same units as R.



# LEAST SQUARES FITTING EXAMPLE

current [mA]	voltage [mV]	voltage error [mV]	voltage measured [mV]	voltage uncertainty [mV]	$x^2$ [mA <sup>2</sup> ]	$xy$ [mA <sup>2</sup> mV]	voltage from fit [mV]
1.0	2.0	-0.8	1.2	1.0	1.0	1.2	2.1
2.0	4.0	0.3	4.3	1.0	4.0	8.6	4.2
3.0	6.0	1.0	7.0	1.0	9.0	20.9	6.3
4.0	8.0	0.0	8.0	1.0	16.0	32.1	8.4
this is "x"					$\Sigma x^2$	$\Sigma xy$	
					30.0	62.9	

This is the true signal

This is the true signal with error (uncertainty).

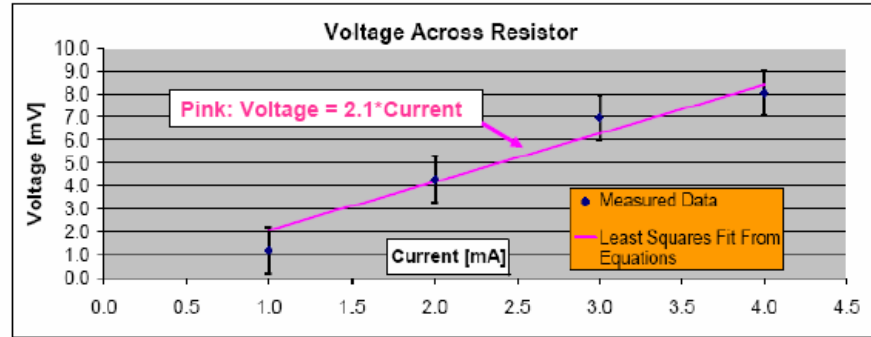
Our model:  $V = I \cdot R$

R from Fit:  $R = \frac{\Sigma(xy)}{\Sigma(x^2)}$       2.1  $\Omega$

What we would measure in real-life

Error in R comes from partial derivative of numerator with respect to y, only

Error in R       $\sigma_R = \sigma_v / \sqrt{\Sigma x^2}$       0.2  $\Omega$



# LEAST SQUARES FITTING

$$y=e^{Ax} \quad y=A+Bx+Cx^2+Dx^3+\dots+Zx^N \quad y=f(x)$$

minimize  $\rightarrow \sum_{j=1}^N (y_j - f(x_j))^2$



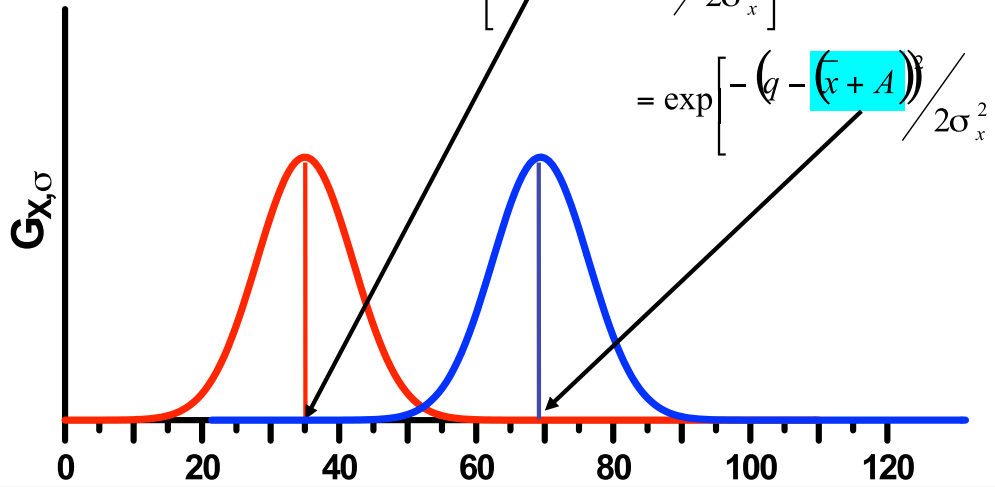
$$\frac{\partial \sum_{j=1}^N (y_j - f(x_j))^2}{\partial A} = 0 \quad \frac{\partial \sum_{j=1}^N (y_j - f(x_j))^2}{\partial B} = 0 \quad \frac{\partial \sum_{j=1}^N (y_j - f(x_j))^2}{\partial C} = 0 \quad \dots$$

$\rightarrow$  **A,B,C...**

$q = x + A$  ||  $q = Bx$  ||  $q = x + y$  || general case

normally distributed  $\rightarrow$   $\text{prob}(x) \propto e^{-\frac{(x - \bar{x})^2}{2\sigma_x^2}}$

$$\begin{aligned} \text{prob}(q) = \text{prob}(x=q-A) &\propto \exp\left[-\frac{((q-A) - \bar{x})^2}{2\sigma_x^2}\right] \\ &= \exp\left[-\frac{(q - (\bar{x} + A))^2}{2\sigma_x^2}\right] \end{aligned}$$



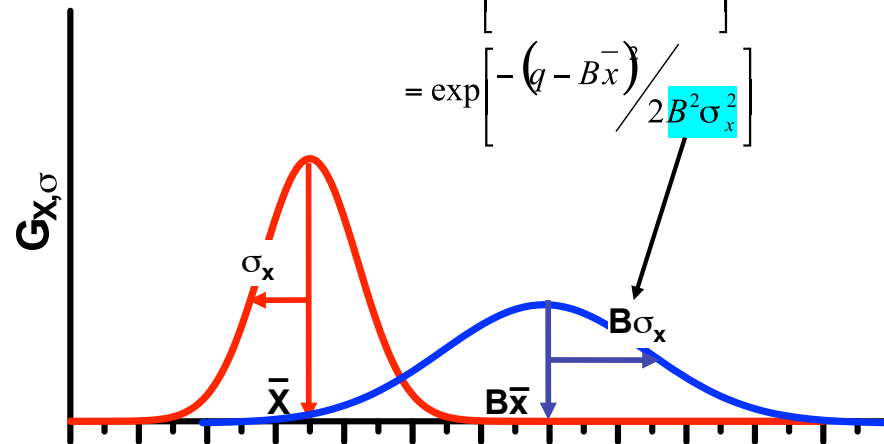
$q = x + A$  ||  $q = Bx$  ||  $q = x + y$  || general case

$\text{prob}(x) \propto e^{-\frac{(x-\bar{x})^2}{2\sigma_x^2}}$


↓  
**normally distributed**

$$\text{prob}(q) = \text{prob}(x=q/B) \propto \exp\left[-\frac{\left(\frac{q}{B} - \bar{x}\right)^2}{2\sigma_x^2}\right]$$

$$= \exp\left[-\frac{(q - B\bar{x})^2}{2B^2\sigma_x^2}\right]$$



$q = x + A$  ||  $q = Bx$  ||  $q = x + y$  || general case


**prob(x and y) = prob(x)\*prob(y)**   $\bar{x} = \bar{y} = 0$

$$\text{prob}(x \& y) \propto \exp\left[-\frac{x^2}{2\sigma_x^2}\right] \exp\left[-\frac{y^2}{2\sigma_y^2}\right] \qquad \text{prob}(x) \propto \exp\left[-\frac{x^2}{2\sigma_x^2}\right]$$

$$= \exp\left[-\frac{1}{2}\left(\frac{x^2}{\sigma_x^2} + \frac{y^2}{\sigma_y^2}\right)\right] \qquad \text{prob}(y) \propto \exp\left[-\frac{y^2}{2\sigma_y^2}\right]$$

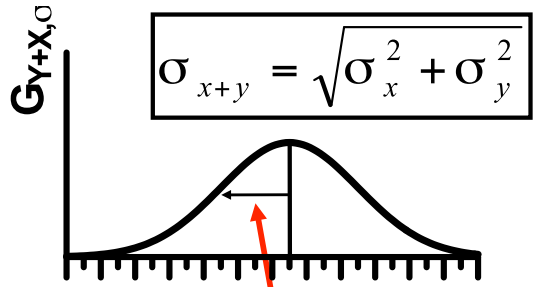
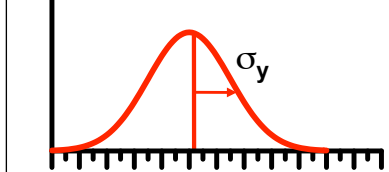
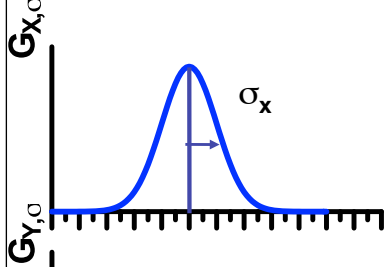
$$\frac{x^2}{A} + \frac{y^2}{B} = \frac{(x+y)^2}{A+B} + \frac{(Bx - Ay)^2}{AB(A+B)} = \frac{(x+y)^2}{A+B} + z^2$$

$$\text{prob}(x \& y) \propto \exp\left[-\frac{(x+y)^2}{2(\sigma_x^2 + \sigma_y^2)} - \frac{z^2}{2}\right]$$



$$\text{prob}(x+y \text{ and } z) \propto \exp\left[-\frac{(x+y)^2}{2(\sigma_x^2 + \sigma_y^2)}\right] \exp\left[-\frac{z^2}{2}\right]$$

$q = x + A$  ||  $q = Bx$  ||  $q = x + y$  || general case



$$\text{prob}(x+y) = \int_{-\infty}^{\infty} \text{prob}(x+y \& z) dz \propto \exp\left[-\frac{(x+y)^2}{2(\sigma_x^2 + \sigma_y^2)}\right] \int_{-\infty}^{\infty} e^{-\frac{z^2}{2}} dz$$

$$\text{prob}(x+y \text{ and } z) \propto \exp\left[-\frac{(x+y)^2}{2(\sigma_x^2 + \sigma_y^2)}\right] \exp\left[-\frac{z^2}{2}\right]$$

$= (2\pi)^{0.5}$

$q = x + A$  ||  $q = Bx$  ||  $q = x + y$  || **general case**

$$q(x,y) \approx \underbrace{q(\bar{x}, \bar{y})}_{\text{fixed number}} + \underbrace{\left(\frac{\partial q}{\partial x}\right)}_{\text{fixed number}} (x - \bar{x}) + \underbrace{\left(\frac{\partial q}{\partial y}\right)}_{\text{normally distributed with } \sigma_x} (y - \bar{y})$$

fixed  
number

fixed  
number

normally distributed  
with  $\sigma_x$

$$\frac{\partial q}{\partial x} \sigma_x$$

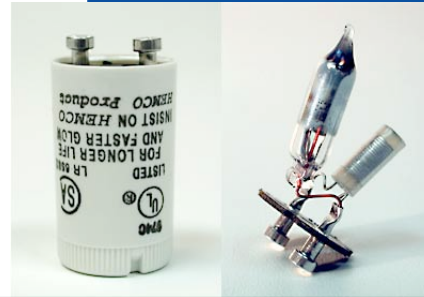
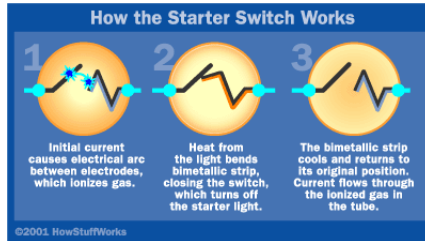
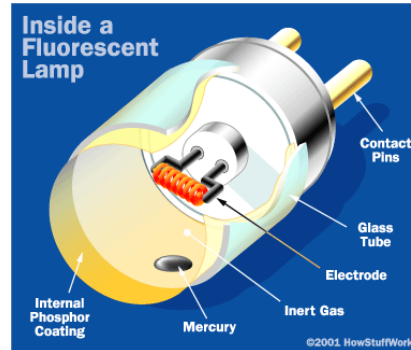
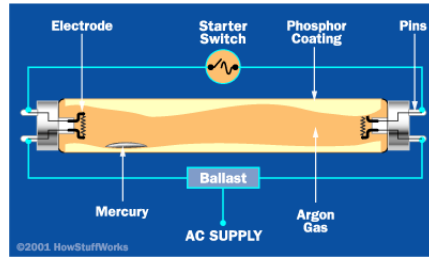
$$\frac{\partial q}{\partial y} \sigma_y$$

$$\sigma_q = \sqrt{\left(\frac{\partial q}{\partial x} \sigma_x\right)^2 + \left(\frac{\partial q}{\partial y} \sigma_y\right)^2}$$

How DAQ can simplify your  
(experimental) life.

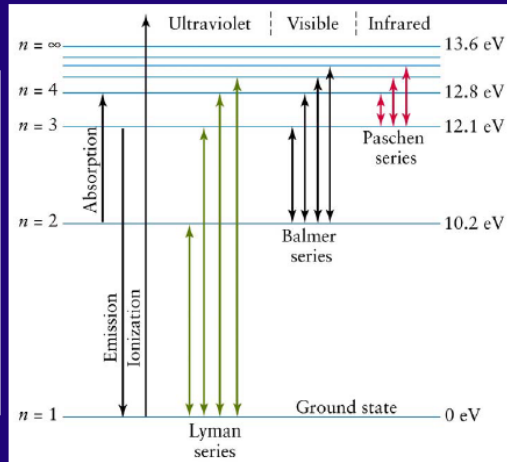
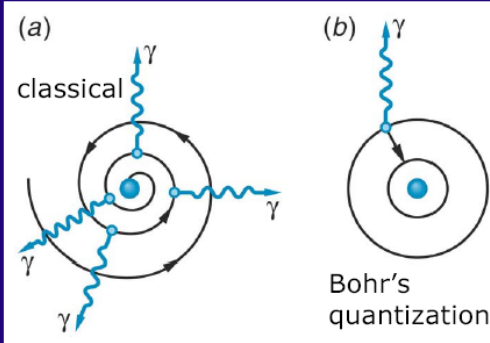


# e<sup>-</sup>-Atom collisions overhead!



# Franck-Hertz Experiment : A prelude

Bohr Atom : Discrete orbit → Emission & Absorption line

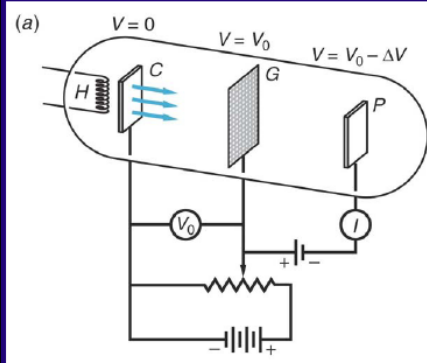


$$r_n = \frac{n^2 \hbar^2}{m k e^2}, \quad n = 1, 2, \dots, \infty$$

$n = 1 \Rightarrow$  Bohr Radius  $a_0$

$$E_n = - \left( \frac{k e^2}{2 a_0} \right) \frac{Z^2}{n^2}$$

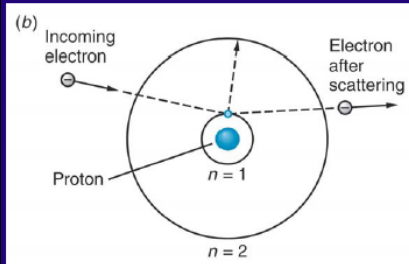
# Franck Hertz Experiment: Playing Football !



Inelastic scattering of electrons  
Confirms Bohr's Energy quantization

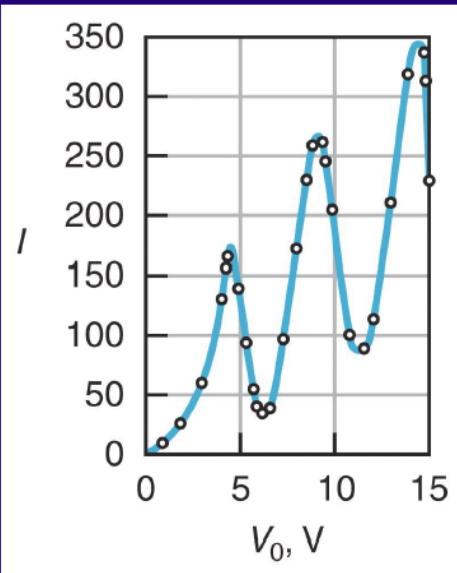
Electrons ejected from heated cathode  
At zero potential are drawn towards  
the positive grid G. Those passing thru  
Hole in grid can reach plate P and cause  
Current in circuit if they have sufficient  
Kinetic energy to overcome the retarding  
Potential between G and P

Tube contains low pressure gas of stuff!



If incoming electron does not have  
enough energy to transfer  $\Delta E = E_2 - E_1$  then  
Elastic scattering, if electron has atleast  
 $KE = \Delta E$  then inelastic scattering and the  
electron does not make it to the plate P  
→ Loss of current

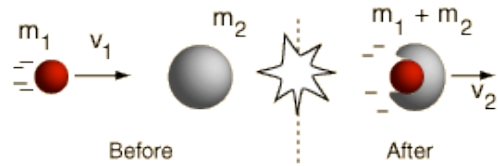
## (J) Franck & (G) Hertz Experiment



Current decreases because many Electrons lose energy due to inelastic Scattering with the Hg atom in tube And therefore can not overcome the Small retarding potential between  $G \rightarrow P$

The regular spacing of the peaks Indicates that ONLY a certain quantity Of energy can be lost to the Hg atom  $\Delta E = 4.9$  eV.

This interpretation can be confirmed Observation of radiation of photon  $e E = hf = 4.9$  eV emitted by Hg atom with  $V_0 > 4.9$  V



	Before		After
Momentum	$m_1 v_1$		$(m_1 + m_2)v_2$
Kinetic energy	$\frac{1}{2} m_1 v_1^2$		$\frac{1}{2} (m_1 + m_2)v_2^2$

From conservation of momentum:

$$m_1 v_1 = (m_1 + m_2)v_2 \Rightarrow v_2 = \frac{m_1}{m_1 + m_2} v_1$$

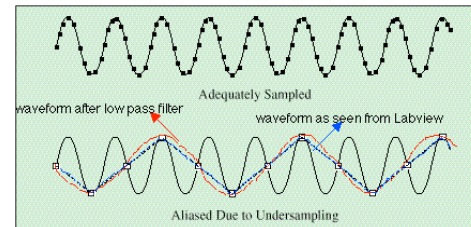
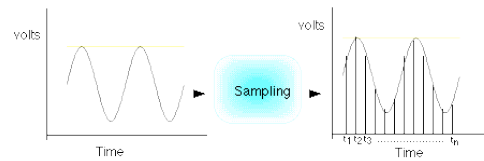
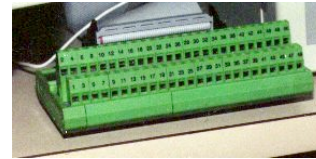
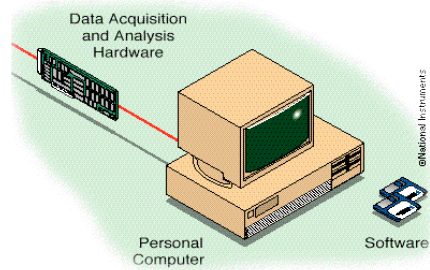
Ratio of kinetic energies before and after collision:

$$\frac{KE_f}{KE_i} = \frac{m_1}{m_1 + m_2}$$

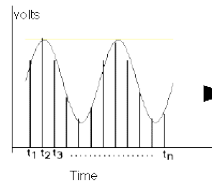
Fraction of kinetic energy lost in the collision:

$$\frac{KE_i - KE_f}{KE_i} = \frac{m_2}{m_1 + m_2}$$

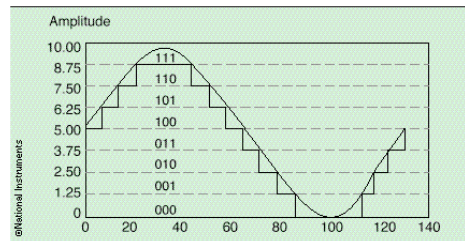
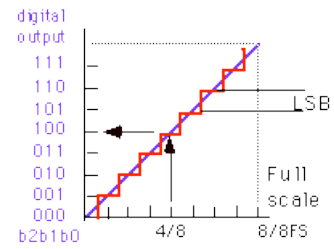
# Electronic Measurement using Digital to Analog Conversion

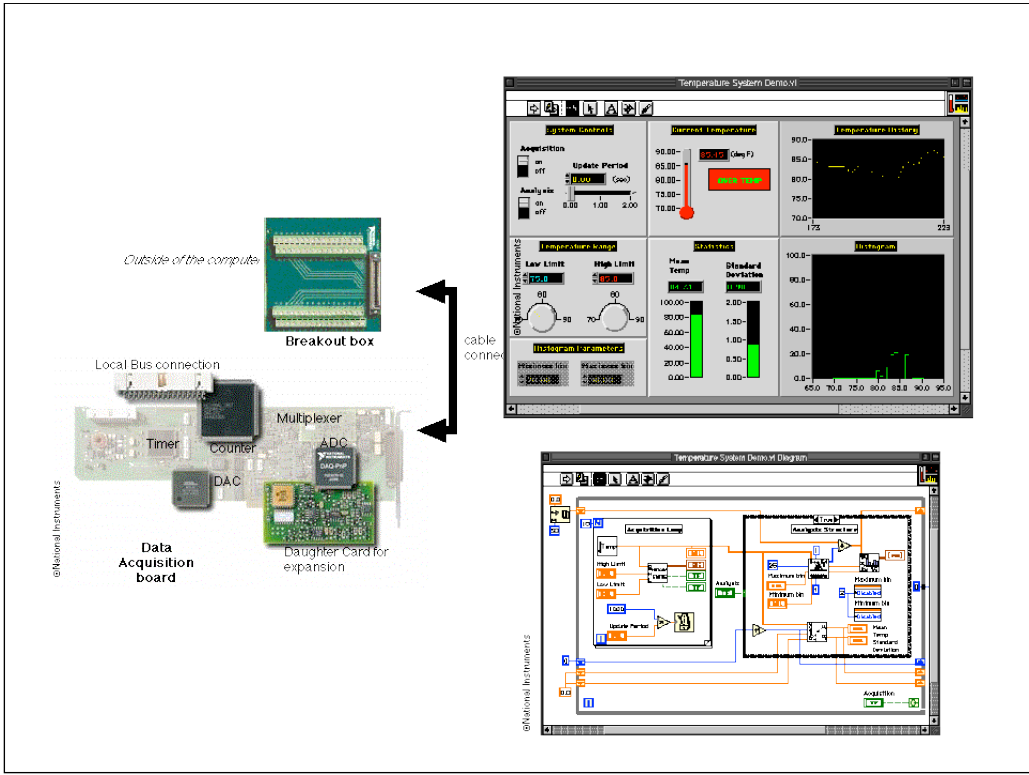


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TIME SAMPLE	DIG CODE
$t_1$	110
$t_2$	111
$t_3$	100
$t_n$	101







# Franck Hertz DAQ

- Program (called a ".vi" file) is on Floppy drive.
- Save data to hard disk, on desktop.
- Email yourself the data from IE
- Save channel 1 data (acceleration voltage)
- Channel 2 is current, measured as a voltage

